



THE CATHOLIC UNIVERSITY OF EASTERN AFRICA

A. M. E. C. E. A

P.O. Box 62157

00200 Nairobi - KENYA

Telephone: 891601-6

Ext 1022/23/25

MAIN EXAMINATION

SEPTEMBER –DECEMBER 2021

FACULTY OF ARTS AND SOCIAL SCIENCES

DEPARTMENT OF ECONOMICS

REGULAR PROGRAMME

ECN 317: MATHEMATICS FOR ECONOMISTS II

Date: DECEMBER 2021

Duration: 2 Hours

INSTRUCTIONS: Answer Question ONE and any TWO Questions

Q1.

a) A company can produce two products, A and B. The profit per unit of A produced is 6 dollars while the profits per unit of B produced is 8 dollars. To produce a unit of A, the company requires 30 labour hours and 20 labour hours for B. The machine hours required are 5 hours and 10 hours for A and B, respectively.

- i) Formulate this problem as a linear programming problem. **(3 Marks)**
 - ii) What should be the optimal production of products A and B. Use simplex method to solve. **(6 Marks)**
 - iii) Formulate the dual problem of the primal problem **(4 Marks)**
- b) Determine whether the following functions are linearly dependent. **(4 Marks)**

$$y_1 = 3x_1^2 + 2x_2^2$$

$$y_2 = 5x_1 + 1$$

- c) Highlight the Kuhn-Tucker necessary conditions for a minimum and a maximum. **(5 Marks)**

d) The supply and demand function of cabbage is given as:

$$Qdt = 125 - 2P_t$$

$$Qst = -50 + 1.5P_{t-1}$$

Required:

- i) Determine the equilibrium price. **(2 Marks)**
- ii) Find general and particular solution. **(4 Marks)**
- iii) Is the price stable? **(2 Marks)**

Q2.

a) Solve the following three simultaneous equations using the gauss Jordan elimination method. **(10 Marks)**

$$X - Z = 4$$

$$2Y - Z = 6$$

$$X + Y = 10$$

b) Differentiate between a homogeneous and a non-homogeneous difference equation. **(4 Marks)**

c) Solve the following difference equations.

i) $Y_{t+1} = 0.2Y_t + 4$ **(3 Marks)**

ii) $Y_{t+1} = 1.2Y_t, Y_0 = 5$ **(3 Marks)**

Q3.

a) With the aid of relevant examples, differentiate between the first-order linear differential function and the second-order third-degree differential function. **(4 Marks)**

b) Determine if the following function is concave or convex.

$$Z = 2x - y - x^2 + 2xy - y^2$$
 (4 Marks)

c) Solve the following maximization problem and show all the necessary Kuhn-Tucker conditions.

(12 Marks)

$$\text{Max } u = xy$$

st.

$$x + y \leq 100$$

$$x \leq 40$$

$$x, y \geq 0$$

Q4.

a) Determine if the following functions are positive definite or negative definite using the Hessian determinants.

i) $Z = 2XY - X^2 + 5Y^2$ **(3 Marks)**

ii) $Z = 200 - 2x^2 - y^2 - 3w - xy - e^{x+y+w}$ **(4 Marks)**

b) Given demand and supply for the cobweb model as follows,

$$Q_{dt} = 22 - 3P_1 \quad Q_{st} = -2 + P_{t-1}$$

Where,

Q_{dt} is quantity demanded and Q_{st} is the quantity supplied.

i) Find the inter-temporal equilibrium prices. **(3 Marks)**

ii) Determine whether the equilibrium is stable. **(4 Marks)**

c) Solve for Y in the following differential equations.

i) $\frac{dy}{dt} = \frac{t}{y}$ **(3 Marks)**

ii) $\frac{dy}{dt} + 2ty = t$ **(3 Marks)**

Q5.

a) Determine if a Cobb-Douglas production function given as $Q = AK^\beta L^\alpha$ is concave or convex given that $\beta + \alpha \leq 1$. **(5 Marks)**

b) Integrate the following functions:

i) $\int (x+3)(x+1)^{\frac{1}{2}} dx$ **(5 Marks)**

ii) $\int x^3 \cdot (\ln x^2) dx$ **(5 Marks)**

iii) $\int 6x^2(x^3+2)^{99} dx$ **(5 Marks)**

END

DTE DEC 2021