



# THE CATHOLIC UNIVERSITY OF EASTERN AFRICA

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**MAIN EXAMINATION**

**JANUARY – APRIL 2019 TRIMESTER**

**FACULTY OF ARTS AND SOCIAL SCIENCES**

**DEPARTMENT OF ECONOMICS**

**REGULAR PROGRAMME**

**ECN 102: INTRODUCTION TO MATHEMATICS FOR ECONOMISTS**

**Date: APRIL 2019**

**Duration: 2 Hours**

**INSTRUCTIONS: Answer Question ONE and any other TWO Questions**

- Q1. a) Describe the following sets using the rule method:
- i.  $F = \{0, 1, 8, 27, 64, 125, 216, \dots\}$  **(2 Marks)**
  - ii.  $G = \{\dots, -30, -20, -10, 0, 10, 20, 30, 40, \dots\}$  **(2 Marks)**
  - iii.  $H = \{1, 2, 3, 5, 7, 11, 13, 17, 19, 23, \dots\}$  **(2 Marks)**
- b) Let  $A = \{1, 2, 3, 4, 5\}$  and  $B = \{0, 3, 6\}$ . Find:
- i)  $A \cap B$  **(2 Marks)**
  - ii)  $A \cup B$  **(2 Marks)**
  - iii)  $A - B$  **(2 Marks)**
  - iv)  $B - A$  **(2 Marks)**
- c) Given a set  $S = \{a, b, c\}$ ,  
Find:
- i)  $P(S)$  **(2 Marks)**
  - ii) The Cardinality of set S. **(2 Marks)**
- d) Let A be the set of students who live one km from school and let B be the set of students who walk to classes. Use the rule method to describe the students in each of following sets:
- i)  $A \cap B$  **(3 Marks)**
  - ii)  $A \cup B$  **(3 Marks)**
  - iii)  $A - B$  **(3 Marks)**
  - iv)  $B - A$  **(3 Marks)**

- Q2. a) Classify all the following numbers as natural, whole, integer, rational, or irrational. List all that apply.
- |      |                |                  |
|------|----------------|------------------|
| i)   | 117            | <b>(2 Marks)</b> |
| ii)  | 0              | <b>(2 Marks)</b> |
| iii) | -12.64039...   | <b>(2 Marks)</b> |
| iv)  | $-\frac{1}{2}$ | <b>(2 Marks)</b> |
| v)   | 6.36           | <b>(2 Marks)</b> |
| vi)  | -3             | <b>(2 Marks)</b> |

- b) Use a well-designed and labeled Venn diagram to show how the numbers listed in (a) above, are classified. Place each number where it belongs on the Venn diagram. **(8 Marks)**

- Q3. a) The final grade a student of economics will get can be expressed in a linear function given here below:

$$G = 5 + 15X + 3Y;$$

Where; G is the final grade in economics

5, is the guaranteed percentage grade

X, is the number of hours studied per week, and

Y, is the number of questions attempted per week.

- i) If the student studied for four hours, and attempted five (5) questions per week, what will be the student's final grade? **(8 Marks)**
- ii) Assume that the General Motor's total cost (TC) and total revenue (TR) functions are given by the following quadratic functions:

$$TC = Q^3 - 16Q^2 + 96Q$$

$$TR = 236Q - 8Q^2$$

What is the profit maximizing output? **(6 Marks)**

What is the maximum profit earned? **(6 Marks)**

- Q4. a) Solve the following simultaneous equations using graphing method:

i)  $4X + 3Y = 11$   
 $2X + Y = 5$  **(4 Marks)**

ii)  $4X + 3Y = -11$   
 $2X + Y = 5$  **(4 Marks)**

- b) If the demand ( $Q_d$ ), and supply ( $Q_s$ ) functions for sausages at the CUEA student center, are given below:

$$Q_d = 50 - P$$
$$Q_s = -10 + 2P$$

- i) What is the market equilibrium price for sausages at the CUEA student Center? **(4 Marks)**
- ii) What is the market equilibrium quantity of sausages at the student Center? **(3 Marks)**
- iii) Using a well labeled diagram, Plot the market equilibrium for CUEA student Center. **(5 Marks)**

- Q5. a) Using different rules of differentiation, find the first derivatives of the following functions:
- i)  $Y = (3X + 5)/(X^2 - 2)$  **(3 Marks)**
- ii)  $Y = (3X^2 + 4X)^{1/2}$  **(5 Marks)**

- b) The monthly demand for T-shirts in Nairobi City is given by;  
 $P = -0.05X + 25$ ; ( $0 < X < 400$ )

Where  $P$  denotes the wholesale unit price in Kenya shillings, and  $X$  denotes the quantity of T-shirts demanded. The monthly cost function for these T-shirts is given as:

$$C(x) = -0.001X^2 + 2X + 200$$

- i) Find the revenue and profit functions **(4 Marks)**
- ii) Find the marginal cost, marginal revenue, and marginal profit functions. **(4 Marks)**
- iii) Find the marginal average cost function **(4 Marks)**

**\*END\***