A. M. E. C. E. A<br>P.O. Box 62157<br>00200 Nairobi - KENYA<br>MAIN EXAMINATION<br>Telephone: 891601-6<br>MAY - JULY 2019 TRIMESTER<br>FACULTY OF SCIENCE

DEPARTMENT OF MATHEMATICS AND ACTUARIAL SCIENCE
REGULAR PROGRAMME
MAT 160: PROBABILTY AND STATISTICS 1

Date: JULY 2019
Duration: 2 Hours
INSTRUCTIONS: Answer Question ONE and any other TWO Questions

Q1. a) Differentiate between the following terms:
i) Probability and statistics
(2marks)
ii) Qualitative and quantitative data
(2marks)
iii) Discrete and continuous variable
(2marks)
iv) Census and sample
b) A coin is tossed three times:
i) Draw a tree diagram to show all the possible outcomes
(2marks)
ii) Find the probability of getting
i) At least one head.
(2marks)
ii) No head
c) In an agriculture Centre, the lengths of a sample of 50 maize cobs were measured and recorded as shown in the table below.

| Length cm | $8-10$ | $11-13$ | $14-16$ | $17-19$ | $20-22$ | $23-25$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No of cobs | 4 | 7 | 11 | 15 | 8 | 5 |

Calculate
i) The mean (3marks)
ii) Semi-inter-quartile range
d) Construct an ungrouped frequency table for the data below.
(6marks) 1614151312141615151417161316151418131517

Q2. a) During a tournament the probability of Miruthu girls winning volleyball, netball, and hockey are $\frac{2}{3}, \frac{\frac{1}{5} \wedge 3}{5}$ respectively. What is the probability that Miruthu girls
i) Wins all three games?
(3marks)
ii) Wins at least one game?
iii) Wins two games
(3marks)
b) The following table shows the results of the test done in Mathematics and Physics.

| Students | A | B | C | D | E | F | G | H |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Mathematics | 63 | 72 | 41 | 56 | 44 | 89 | 70 | 45 |
| Physics | 48 | 71 | 50 | 46 | 35 | 92 | 42 | 48 |

Calculate the product-moment correlation coefficient and comment on the result obtained.
(11marks)

Q3. a) This frequency distribution shows the number of pounds of each snack food eaten during the Super Bowl. Construct a pie chart for the data.
(7marks)

| snack | Potato <br> chips | Tortilla <br> chips | pretzels | popcorn | Snack <br> nuts |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Pounds <br> in <br> millions | 11.2 | 8.2 | 4.3 | 3.8 | 2.5 |

b) A sample of 250 students was asked to indicate their favorite TV channels and their responses were as follows:

| TV station | KBC | NTV | CITIZEN | KTN | FAMILY |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Number of <br> viewers | 28 | 52 | 92 | 63 | 15 |

c) $\quad$ A bag $B_{1}$ has 3 mangoes and 5 oranges and bag $B_{2}$ has 9 mangoes and 3oranges. A bag is selected where bag $B_{1}$ selected with probability of $3 / 5$ and $\operatorname{bag} B_{2}$ with probability $2 / 5$. Two fruits are selected without replacement.

Draw a tree diagram and show the probability of the possible events.
(8 marks)

Q4. a) Using the following information $8,3,9,15,12,4,8$.
(5marks)
Show that $\bar{X}_{H} \leq \bar{X}_{g} \leq \bar{X} \quad$ Where
$\bar{X}_{H}:$ Harmonicmean
$\bar{X}_{g}$ : Geometricmean
$\bar{X}:$ Arithmetic mean
b) The table below relates the variables $X$ and $Y$

| X | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 9 | 18 | 23 | 29 | 32 | 31 | 35 | 42 | 48 |

Find

| i) | the correlation coefficient | (7marks) |
| :--- | :--- | :--- |
| ii) | The value of $a$ and $b$ | (4marks) |
| iii) | $Y$ if $X=15$ | $(\mathbf{2 m a r k s})$ |
| iv) | $X$ if $Y=62$ | $(2$ marks) |

Q5. a) A company employs skilled and unskilled workers. 30\% are skilled workers and the rest unskilled the probability that of skilled worker will finish the job on time is 0.72 and the probability that the unskilled worker will finish on time is 0.48 .
Given that a job was completed on time, what is the probability that the job was done by unskilled work?
(8marks)
b) Construct a histogram, frequency polygon, and an ogive for the distribution shown of the miles that 20 randomly selected runners ran during a given week.
(12marks)

| class | $6-10$ | $11-15$ | $16-20$ | $21-25$ | $26-30$ | $31-35$ | $36-40$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| frequenc <br> $y$ | 1 | 2 | 3 | 5 | 4 | 3 | 2 |

*END*

