THE CATHOLIC UNIVERSITY OF EASTERN AFRICA

A. M. E. C. E. A

P.O. Box 62157 00200 Nairobi - KENYA Telephone: 891601-6 Fax: 254-20-891084 E-mail:academics@cuea.edu

MAIN EXAMINATION

AUGUST - DECEMBER 2018 TRIMESTER

FACULTY OF COMMERCE

DEPARTMENT OF ACCOUNTING AND FINANCE

REGULAR / ODEL PROGRAMME

CID 072: FOUNDATIONS OF BUSINESS MATHEMATICS

Date: DECEMBER 2018 Duration: 2 Hours
INSTRUCTIONS: Answer Question ONE and ANY OTHER TWO Questions

- Q1. a) Distinguish between any of the following terms using suitable examples
 - i) Classical Probability and Frequency Probability
 - ii) Union of a set and intersection of a set
 - iii) Universal set and empty set

(6marks)

b) Given the functions $f(x) = x^2 - 3$ and g(x) = 4x + 7, use the rules of algebra of functions to work out;-

$$i)(f+g)(x)$$

$$ii)(f,g)(x)$$

 $iii)(f \div g)(x)$ (6marks)

c) Solve for x in each of the following

$$3x^2 + 13x - 10$$

(3marks)

d) Solve the following Simultaneous equation using Gaussian elimination method (9marks)

$$2x + y + 3z = -2x - y - z = -33x - 2y + 3z = -12$$

e) For each of the following sets of revenue (TR) and total cost equations (TC), Express π as a function of output x and then determine the maximum output level by finding the vertex of the Parabola.

$$i)TR = -6x^2 + 1200x, TC = 180x + 3350$$

(3marks)

- Q2. a) The demand function of a firm is given, as P = 50 0.5q. Given that, P is the Price and q is the number of commodities;
 - i) Write down the equation of the total Revenue Function

(2marks)

- ii) Graph the total revenue for $0 \le P \le 100$ (5marks)
- iii) Estimate the value of q for which the total revenue is maximum and give the value of the total revenue (3marks)
- b) A computer retailer conducted a survey of 250 clients and obtained the information shown.

Gender	AGE		
	Less than 25	25-40	41 and over
Male	70	25	50
UFemale	45	40	20

If a customer is selected at random, find the following probabilities;

- i) The customer is a female aged 25-40. (2marks)
- ii) The Customer is male (1mark)
- iii) If the selected customer is less than 25, what is the probability that they are female? (4marks)
- iv) Are the events aged 25-40 and female, Independent?

(3marks)

Q3. a) Use Matrices find the equilibrium values for x, y and z given the following first order conditions. (10marks)

$$10x - 2y - z = 0
-2x + 16y - z = 0
60 - x - y = 0$$

- b) A manufacturer makes two products x_1 and x_2 . The first requires 5hours for processing, 3hours for assembling and 4 hours for packaging. The second requires 2 hours for processing, 12 hours for assembling and 8 hours for packaging. The plant has 40 hours available for processing, 60 hours available for assembling and 48 hours available for packaging. The profit margin for x_1 is sh. 700 and that of x_2 is sh. Sh. 2100.
 - i) Express the data in equations necessary to determine the output pairs that will maximize profits (3marks)
 - ii) Use the graph paper provided or otherwise to identify the pair that gives maximum profit, and hence give the value of maximum profit (7marks)

- Q4. a) A nutritionist wishes her clients to have a daily minimum of 30 units of Vitamin A, 20 units of Vitamin D, and 24 units of Vitamin E. One dietary supplement y₁ costs sh. 800 per kg and provides 2 units of Vitamin A, 5 units of Vitamin D and 2 units of Vitamin E. A second supplement y₂ Costs sh. 1600 per kg and provides 6 units of Vitamin A, 1 Unit of Vitamin D and 3 Units of Vitamin E. Workout the least cost of combinations of Supplements meeting daily requirements. (10marks)
 - b) In a recent survey, people were asked if they took a vacation in the summer, winter, or spring in the past year. The results were, 73 took a vacation in the summer, 51 took a vacation in the winter, 27 took a vacation in the spring and 2 had taken no vacation. In addition, 10 had taken vacations at all three times, 33 had taken both a summer and a winter vacation, 18 had taken only a winter vacation, and 5 had taken both a summer and spring but not a winter vacation.
 - i) Draw a Venn diagram for the information
 - ii) How many people were surveyed?
 - iii) How many people had taken vacations at exactly two times of the year?
 - iv) How many people had taken vacations during at most one time of the year?
 - v) What percentage, had taken vacations, during both summer and winter but not spring? (10marks)

END