A. M. E. C. E. A

MAIN EXAMINATION
AUGUST - DECEMBER 2018 TRIMESTER
FACULTY OF COMMERCE
DEPARTMENT OF ACCOUNTING AND FINANCE
REGULAR / ODEL PROGRAMME
CID 072: FOUNDATIONS OF BUSINESS MATHEMATICS
Date: DECEMBER 2018
Duration: 2 Hours
INSTRUCTIONS: Answer Question ONE and ANY OTHER TWO Questions

Q1. a) Distinguish between any of the following terms using suitable examples
i) Classical Probability and Frequency Probability
ii) Union of a set and intersection of a set
iii) Universal set and empty set
(6marks)
b) Given the functions $f(x)=x^{2}-3$ and $g(x)=4 x+7$, use the rules of algebra of functions to work out;-
$i)(f+g)(x)$
ii) $(f . g)(x)$
iii) $(f \div g)(x)$
(6marks)
c) Solve for x in each of the following

$$
\begin{equation*}
3 x^{2}+13 x-10 \tag{3marks}
\end{equation*}
$$

d) Solve the following Simultaneous equation using Gaussian elimination method
(9marks)

$$
\begin{gathered}
2 x+y+3 z=-2 \\
x-y-z=-3 \\
3 x-2 y+3 z=-12
\end{gathered}
$$

e) For each of the following sets of revenue (TR) and total cost equations (TC), Express $\pi$ as a function of output $x$ and then determine the maximum output level by finding the vertex of the Parabola.

$$
\begin{equation*}
i) T R=-6 x^{2}+1200 x, T C=180 x+3350 \tag{3marks}
\end{equation*}
$$

ii) $T R=-4 x^{2}+900 x, T C=600 x+12,500$

Q2. a) The demand function of a firm is given, as $P=50-0.5 q$. Given that, P is the Price and q is the number of commodities;
i) Write down the equation of the total Revenue Function
(2marks)
ii) Graph the total revenue for $0 \leq P \leq 100$
(5marks)
iii) Estimate the value of $q$ for which the total revenue is maximum and give the value of the total revenue (3marks)
b) A computer retailer conducted a survey of 250 clients and obtained the information shown.

| Gender | AGE |  |  |
| :--- | :--- | :--- | :--- |
|  | Less than 25 | $25-40$ | 41 and over |
| Male | 70 | 25 | 50 |
| UFemale | 45 | 40 | 20 |

If a customer is selected at random, find the following probabilities;
i) The customer is a female aged 25-40.
ii) The Customer is male
iii) If the selected customer is less than 25 , what is the probability that they are female?
(4marks)
iv) Are the events aged 25-40 and female, Independent?
(3marks)
Q3. a) Use Matrices find the equilibrium values for $x, y$ and $z$ given the following first order conditions.
(10marks)

$$
\begin{gathered}
10 x-2 y-z=0 \\
-2 x+16 y-z=0 \\
60-x-y=0
\end{gathered}
$$

b) A manufacturer makes two products $\mathrm{x}_{1}$ and $\mathrm{x}_{2}$. The first requires 5hours for processing, 3hours for assembling and 4 hours for packaging. The second requires 2 hours for processing, 12 hours for assembling and 8 hours for packaging. The plant has 40 hours available for processing, 60 hours available for assembling and 48 hours available for packaging. The profit margin for $x_{1}$ is sh. 700 and that of $x_{2}$ is sh. Sh. 2100.
i) Express the data in equations necessary to determine the output pairs that will maximize profits
ii) Use the graph paper provided or otherwise to identify the pair that gives maximum profit, and hence give the value of maximum profit
(7marks)

Q4. a) A nutritionist wishes her clients to have a daily minimum of 30 units of Vitamin A, 20 units of Vitamin D, and 24 units of Vitamin E. One dietary supplement y1 costs sh. 800 per kg and provides 2 units of Vitamin A, 5 units of Vitamin D and 2 units of Vitamin E. A second supplement y2 Costs sh. 1600 per kg and provides 6 units of Vitamin A, 1 Unit of Vitamin D and 3 Units of Vitamin E. Workout the least cost of combinations of Supplements meeting daily requirements.
(10marks)
b) In a recent survey, people were asked if they took a vacation in the summer, winter, or spring in the past year. The results were, 73 took a vacation in the summer, 51 took a vacation in the winter, 27 took a vacation in the spring and 2 had taken no vacation. In addition, 10 had taken vacations at all three times, 33 had taken both a summer and a winter vacation, 18 had taken only a winter vacation, and 5 had taken both a summer and spring but not a winter vacation.
i) Draw a Venn diagram for the information
ii) How many people were surveyed?
iii) How many people had taken vacations at exactly two times of the year?
iv) How many people had taken vacations during at most one time of the year?
v) What percentage, had taken vacations, during both summer and winter but not spring?

## *END*

