


How would the overall project completion time be affected by an increase in the completion time for activity 1 of 2 weeks?
(2marks)
f) Customers arrive at a bank at a Poisson rate $\lambda / h r$. Suppose that two customers arrive during the first hour. What is the probability that;
i) Both arrived during the first 20 minutes?
(2marks)
ii) At least one arrived during the first 20 minutes?
(2marks)
g) Construct a network for the project whose activities and their precedence relationships are given below;

| Activity | A | B | C | D | E | F | G | H | I |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Immediate <br> Predecessor | - | - | A,B | B | B | A,B | F,D | F,D | C,G |

(4marks)
Q2. a) The following table shows the jobs of a network along with their time estimates. The time estimates are in days:

| Job | $\mathbf{1 - 2}$ | $\mathbf{1 - 6}$ | $\mathbf{2 - 3}$ | $\mathbf{2 - 4}$ | $\mathbf{3 - 5}$ | $\mathbf{4 - 5}$ | $\mathbf{5 - 8}$ | $\mathbf{6 - 7}$ | $\mathbf{7 - 8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a | 3 | 2 | 6 | 2 | 5 | 3 | 1 | 3 | 4 |
| m | 6 | 5 | 12 | 5 | 11 | 6 | 4 | 9 | 19 |
| b | 15 | 14 | 30 | 8 | 17 | 15 | 7 | 27 | 28 |

i) Draw the project network
(6marks)
ii) Find the critical path
(3marks)
iii) Find the probability that the project is completed in 31 days.
(4marks)
b) Determine the initial basic feasible solution for the following TP, using the Least Cost Method

|  | $D_{1}$ | $D_{2}$ | $D_{3}$ | $D_{4}$ | Supply |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $O_{1}$ | 6 | 4 | 1 | 5 | 14 |
| $O_{2}$ | 8 | 9 | 2 | 7 | 16 |
| $O_{3}$ | 4 | 3 | 6 | 2 | 5 |
| Demand | 6 | 10 | 15 | 4 | 35 |

(7marks)
Q3. a) Find the initial basic feasible solution for the following transportation problem using the Vogel's Approximation Method

| Destination |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Factory |  | $D_{1}$ | $D_{2}$ | $D_{3}$ | $D_{4}$ | Supply |
|  | $F_{1}$ | 3 | 3 | 4 | 1 | 100 |
|  | $F_{2}$ | 4 | 2 | 4 | 2 | 125 |
|  | $F_{3}$ | 1 | 5 | 3 | 2 | 75 |
|  | Demand | 120 | 80 | 75 | 25 | 300 |

b) Arrivals in a telephone booth are considered to be Poisson with an average time of 10 minutes between one arrival and the next. The length of a telephone call is assumed to be distributed exponentially with mean 3 minutes.
i) What is the probability that a person arriving at the booth will have to wait?
(3marks)
ii) What is the average length of the queue that forms from time to time?
(3marks)
iii) The telephone department will install a second booth when convinced that an arrival would except to have to wait at least three minutes for the phone. By how much must the flow of arrivals be increased in order to justify second booth?
(4marks)

Q4. a) Four different jobs can be done on four different machines and take down time costs are prohibitively high for change over's. The matrix below gives the cost in Kenya Shillings ('000) of producing job $i$ on machine $j$ :

| Jobs | Machine |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | $M_{1}$ | $M_{2}$ | $M_{3}$ | $M_{4}$ |
| $J_{1}$ | 5 | 7 | 11 | 6 |
| $J_{2}$ | 8 | 5 | 9 | 6 |
| $J_{3}$ | 4 | 7 | 10 | 7 |
| $J_{4}$ | 10 | 4 | 8 | 3 |

How should the jobs be assigned to the various machines so that the total cost is minimized.
(10marks)
b) Consider the queuing model $(M / M / 1):(\infty / F C F S)$
i) Explain clearly the meaning of each symbol in the model
(3marks)
ii) If in such a model $p_{n}=(1-\rho) \rho^{n}$ where $\rho=\lambda / \mu<1, n=1,2, \ldots$, show that $L_{s}=\frac{\rho}{1-\rho}$ where $L_{s}$ is the expected number of units in the system.
(7marks)
Q5. a) Tasks $A, B, \ldots, H, I$ constitute a project. The notation $X<Y$ means that the task $X$ must be completed before Yis started.
With the notation,
$A<D, A<E, B<F, D<F, C<G, C<H, F<I, G<I$
Draw a graph to represent the sequence of tasks and find the minimum time of completion of the project, when the time (in days) of completion of each task is as follows.
The above constraints can be given in the following table

| Task | A | B | C | D | E | F | G | H | I |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Time (days) | 8 | 10 | 8 | 10 | 16 | 17 | 18 | 14 | 9 |

(10marks)
b) Use dynamic programming to solve the LPP
$\operatorname{Max} . Z=x_{1}+9 x_{2}$
Subject to the constraints
$2 x_{1}+x_{2} \leq 25$
(10marks)
$x_{2} \leq 11$
$x_{1}, x_{2} \geq 0$
*END*

