



THE CATHOLIC UNIVERSITY OF EASTERN AFRICA

A. M. E. C. E. A

MAIN EXAMINATION

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AUGUST - DECEMBER 2016 TRIMESTER

FACULTY OF ARTS AND SOCIAL SCIENCES

DEPARTMENT OF SOCIAL SCIENCES

REGULAR PROGRAMME

SEC 102: INTRODUCTION TO MATHEMATICS FOR ECONOMISTS

Date: DECEMBER 2016

Duration: 2 Hours

INSTRUCTIONS: Answer Question ONE and ANY other TWO Questions

Question 1

a.) Describe the following sets using the list method and give the set Cardinality:

i. $A = \{x/x \text{ is a natural number which is 1 less than a multiple of 3}\}$

(2 Marks)

ii. $B = \{y/y \text{ is a rational number whose value is } 1/3\}$

(2 Marks)

iii. $C = \{n/n \text{ is a vowel that appears in the phrase "set of consonants"}\}$

(2 Marks)

iv. $D = \{z/z \text{ is an even prime number greater than 2}\}$

(2 Marks)

b.) Given a universal set: $U = \{1, 2, 3, 4, 5, 6\}$,

And Sets: $A = \{1, 2, 3\}$; $B = \{3, 4, 5, 6\}$. Find:

$A \cap B$;

ii. $A \cup B$;

iii. $B - A$;

iv. B'

(4 Marks)

v. Represent your answers in "b" above by a Venn diagram in each case.

(3 Marks)

c.) Given a set $S = \{0, 1, 2\}$,

Find:

- | | | |
|----|---------------------------|------------------|
| i. | $P(S)$ | (4 Marks) |
| ii | The Cardinality of set S. | (1 Mark) |

d.) Statements A and B are defined as follows:

A = The Airways is operating at a loss

B = The Airways will shut down its office.

Use various set symbols to represent the following statements:

i. The Airways is operating at a loss and it will shut down its office
(5Marks)

ii The Airways is operating at a loss, but it will not shut down its office.
(5Marks)

Question 2

a.) Let x and y be rational and irrational numbers respectively,

i. Is $x + y$, necessarily an irrational number? Give an example in support of your answer.
(5 marks)

li Is $x.y$ necessarily an irrational number? Justify your answer
(5 Marks)

b.) Plot the following real number sets:

i. $A = \{ \text{Whole numbers} \}$ **(3 Marks)**

ii. $B = \{ \text{Integers} \}$ **(3 Marks)**

iii. $A \cap B$. **(4 Marks)**

Question 3

a.) Use any exponents' and/or logarithms' rules to simplify the following:

i. $x = y^{1/4} \times y^{3/4}$ **(1.5 marks)** iv. $n = (x^{3/4})^8$ **(1.5 marks)**

ii. $y = x^2 / x^{3/2}$ **(1.5 marks)** v. $M = x^2 y^3 / x^4 y$ **(1.5 marks)**

iii. $x = \log_3 9$ **(1.5 marks)**

vi. $X = \log_4 2$ **(1.5 marks)**

b.) Find the value of x in log form:

I. $5^x = 2(3)^x$ **(5 Marks)**

II. If Kenya's National Income was 3 trillion in 2014; and assume that it grew at 4% per year; what will be Kenya's National Income in the year 2034?

(6 Marks)

Question 4

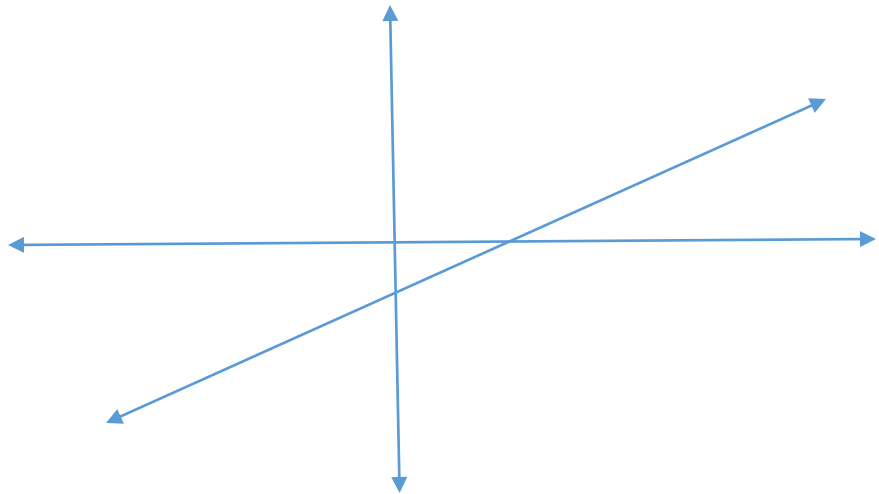
a.) i. Distinguish between a "Relation" and a "Function" **(2 Marks)**

ii. Relations can be written in several ways; ordered pairs, table, graphs, or mapping. Give examples of each of these ways.

(6 Marks)

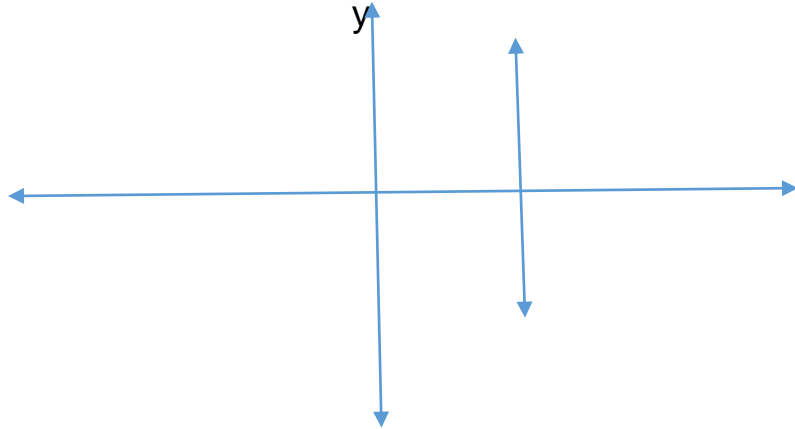
b) Does the following graph represent a function? If yes, name the domain and range.

i.



(2 marks)

ii.



(2 marks)

c) Find the value of x in the following functions:

i) $f(x) = x - 2$

(2 marks)

ii) $f(x) = 2x + 3$; find $f(-2)$

(2 marks)

iii. $f(x) = x^2 - x + 7$; find $f(2y)$

(2 marks)

iv. $f(x) = x^2 - 3$; find $f(a - 1)$

(2 marks)

Question 5.

a.) i. Solve the following simultaneous equations by graphical method:

$$4x + 3y = 11$$

$$4x + y = 5$$

(2 Marks)

ii. Given the demand and supply equations below:

$$Q_d = 30 - P$$

$$Q_s = -20 + 3P$$

Where:

Q_d is quantity demanded

Q_s is quantity supplied, and P is the price level. If the equilibrium in the market is attained when $Q_d = Q_s$; what is the equilibrium quantity and equilibrium price?

(8 Marks)

b.) Find the derivatives of the following equations:

i. $y = (x^2 + 3) (2x^3 + x^2 - 3)$

(5 Marks)

ii. $y = x^{1/2} / 2 + x^5$

(5 Marks)

END