



THE CATHOLIC UNIVERSITY OF EASTERN AFRICA

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MAIN EXAMINATION

SEPTEMBER –DECEMBER 2021

FACULTY OF SCIENCE

DEPARTMENT OF MATHEMATICS

REGULAR PROGRAMME

MAT 364: DESIGN AND ANALYSIS OF SAMPLE SURVEY

Date: DECEMBER 2021

Duration: 2 Hours

INSTRUCTIONS: Answer Question ONE and any TWO Questions

Q1.

- a) Define the following terms **(3 Marks)**
- Sample survey
 - Estimator
 - Bias
- b) State and explain the properties of a BEST estimator. **(7 Marks)**
- c) State and describe the four types of non-sampling error. **(8 Marks)**
- d) From a population of size 5, calculate the number of samples of size 2 that can be drawn using
- SRSWR.
 - SRSWOR. **(2 Marks)**
- e) The depth Y of the roots of plants in a field is uniformly distributed between 5cm and 8cm with the probability density function $f(y) = \frac{1}{3}, \forall 7 < y < 10$. Estimate the average length of roots of the plants with an accuracy of relative standard error of 2%. What is the required minimum with replacement sample size n? **(4 Marks)**

f) Suppose a population consists of $N=4$ units. The variable Y_i takes values 1,2,3,4.
Calculate:

- i) The populations mean square error. **(3 Marks)**
ii) population variance **(3 Marks)**

Q2. The following data shows daily yield of two types of cows in litres per day.

| S.No | Type | Yield |
|------|------|-------|
| 1 | A | 43 |
| 2 | B | 49 |
| 3 | A | 47 |
| 4 | A | 42 |
| 5 | B | 52 |
| 6 | A | 49 |
| 7 | A | 44 |
| 8 | B | 54 |
| 9 | A | 48 |
| 10 | A | 45 |
| 11 | A | 47 |
| 12 | A | 52 |
| 13 | B | 50 |
| 14 | A | 49 |
| 15 | B | 63 |
| 16 | A | 44 |
| 17 | A | 46 |
| 18 | B | 56 |
| 19 | A | 50 |
| 20 | A | 48 |
| 21 | B | 50 |

- a) If we select a *SRSWOR* sample of 4 units, find the variance of the estimator of population mean. **(8 Marks)**
- b) If we stratify the population on the basis of type, and then select 2 units from each type, find the variance of the estimator of mean in stratified sampling. (Let type *B* take stratum 1 and type *A* take stratum2). **(12 Marks)**

Q3. Consider a population consisting of the following six units.

| Unit | A | B | C | D | E | F |
|-------|-----|-----|------|------|------|-----|
| Value | 718 | 912 | 1014 | 1113 | 1110 | 615 |

Consider the following sampling plan.

| Sample number | samples | Probability |
|---------------|---------|-------------|
| 1 | ACE | 1/9 |
| 2 | ACF | 1/9 |
| 3 | ADE | 1/9 |
| 4 | ADF | 1/9 |
| 5 | BCE | 1/9 |
| 6 | BCF | 1/9 |
| 7 | BDE | 1/9 |
| 8 | BDF | 1/9 |
| 9 | CDF | 1/9 |

Use the above tables to compute the following.

- a) $E(\bar{y}_t)$ **(16 Marks)**
- b) $B(\bar{y}_t)$ **(2 Marks)**
- c) $MSE(\bar{y}_t)$ **(2 Marks)**

Q4. An experienced farmer makes an eye estimate of the weight of peaches x_i on each tree in an orchard of $N=200$ trees with population mean $\bar{X}=58$. The peaches are picked and weighed on a simple random sample of 10 trees, with the following results:

| Tree | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | Total |
|------------------|----|----|----|----|----|----|----|----|----|----|-------|
| Actual wt, y_i | 61 | 42 | 50 | 58 | 67 | 45 | 39 | 57 | 71 | 53 | 543 |
| Est. wt, x_i | 59 | 47 | 52 | 60 | 67 | 48 | 44 | 58 | 76 | 58 | 569 |

Apply the ratio method of estimation to estimate:

- a) The average actual weight. **(4 Marks)**
- b) An estimator of the mean square error of the ratio estimator. **(13 Marks)**
- c) Hence deduce the 95% confidence interval. **(3 Marks)**

Q5. A company selected a SRSWOR sample of six varieties of a product out of 70 varieties available in the market as shown below.

| Variety | <i>A</i> | <i>B</i> | <i>C</i> | <i>D</i> | <i>E</i> | <i>F</i> |
|--------------|----------|----------|----------|----------|----------|----------|
| No. of items | 855 | 940 | 90 | 46 | 20 | 16 |

- a) Estimate the average number of items in each variety. **(3 Marks)**
- b) Construct a 95% confidence interval for the average number of items in each variety. **(12 Marks)**
- c) Estimate the total number of items in the market. **(2 Marks)**
- d) Construct a 95% confidence interval for the total number of items in the market. **(3 Marks)**

END